

THE MULTIPLEXING OF OFDM SIGNALS ON THE DOWNLINK IN UTRAN-FDD

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ABSTRACT

The UMTS network is complementary to GSM and GPRS. The GSM network covers the features required for voice-type services in a circuit mode, the network brings GPRS the first features to the introduction of services such as packet data, and UMTS networks complement these by offering voice and data services on an additional packet. UMTS is thus an extension of GPRS and also works in packet mode. The transmission speed offered by UMTS networks to 2Mbit/s. UMTS infrastructure enables expansion of frequencies as well as changes in data coding. In this paper, the use of OFDM signals in the UMTS access network UTRAN-FDD and 64QAM modulation allowed us to improve the rate 2Mbit/s to 22.5 Mbit/s. The results, including improved throughput to 22.5Mbit/s, show us that the power frequency spectrum of a single OFDM signal is centered around the fundamental frequency, but the spectral width of the power spectrum of the OFDM signals is higher than that of the power spectrum is a function that is typically used in UMTS. We also noted that the greater the number of carriers increases, the more important the spectral width is. The multicarrier modulation was based, in our case, on the choice of the multiplexing of signals without noise and with noise.

KEYWORDS

OFDM, UMTS, UTRAN-FDD, Multiplexing

1- INTRODUCTION

The problem that arises in the cellular network is the low flow for packet communications. The cellular network of third-generation UMTS (Universal Mobile Telecommunications System) could satisfy mobile users, by adding services such as access to wireless internet, video telephony, and video messages as well as the reception of television on the phone. But the access network, the UTRAN (UMTS Terrestrial Radio Access Network), the latter, achieves a maximum flow of 2Mbit/s per user, which is insufficient for advanced applications, bandwidth-intensive.

Moreover, wireless networks like WiFi[1] are normalized by offering much higher data rates than UMTS, up to 500Mbit/s and therefore allow high-bandwidth applications, like multimedia, for example.

To overcome these difficulties, we suggest a reform of the UTRAN in view of using orthogonal carriers in OFDM, instead of a gate function.

We use the multicarrier techniques, which include transmitting digital data, by modulating a number of carriers simultaneously. We applied these techniques to signals without noise and with noise.

2- MULTIPLEXING OF SIGNALS WITHOUT NOISE

We consider at the level of a transmitter given, the following hypothesis: k users want to send information (signals) via a common carrier broadband. Each information is modeled by a sequence of ± 1 . Let $g_k(t)$ the pseudo-random signal with T the length of information bit and T_c the chip duration of pseudo-random code with $T = L \cdot T_c$ (1)

In which L is the number of chip used at the spreading sequence.

$$\begin{cases} g_k(t) = \sum_{n=0}^{L-1} a_k(n) \cdot \text{ofdm}_n(t - nT_c) \\ \text{for } 0 \leq t \leq T \end{cases} \quad (2)$$

With:

- $\{a_k\}$ a pseudo-random a_k is ± 1 .
- $\text{ofdm}(t) = \sum_{i=0}^{N-1} C_i e^{j2\pi f_i t}$ is the total signal of all data from one OFDM symbol.
- C_i complex numbers that carry information, defined from bits by a constellation quadrature amplitude modulation (QAM) in multiple states $(4, 16, 64, \dots, 2^q)$. Assuming $C_i = \alpha_i + j\beta_i$ then $\text{ofdm}(t) = \sum_{i=0}^{N-1} (\alpha_i + j\beta_i) e^{j2\pi f_i t}$ (3)

We multiplexe the information by combining each with a vector g_k . Thus we get the packet of bits of length N : $b_k = [b_k(1), \dots, b_k(N)]^t$. The signal becomes:

$$s_k(t) = \sqrt{\xi_k} \sum_{m=1}^M b_k(m) g_k(t - mT)$$

In which ξ represents the signal energy per byte and $b_k(m)$ is the spreading code that handles the multiplexing of multiple channels from a single source. Each source can use all codes.

$$g_k(t - mT) = \sum_{n=0}^{N-1} a_k(n) \cdot \text{ofdm}_n\left(t - \left(m + \frac{n}{L}\right)T\right)$$

$$g_k(t - mT) = \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} C_i e^{j2\pi f_i \left(t - \left(m + \frac{n}{L}\right)T\right)} \quad (5)$$

$$s_k(t) = \sqrt{\xi_k} \sum_{m=1}^M b_k(m) \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} C_i e^{j2\pi f_i \left(t - \left(m + \frac{n}{L}\right)T\right)} \quad (6)$$

Then we couple all users and the signal becomes :

$$S(t) = \sum_{k=1}^K s_k(t - \tau_k) \text{ with } 0 \leq \tau_k < T \text{ for } 1 \leq k \leq K \quad (7)$$

And τ_k represents the transmission delay for user k. If we consider that the signals are synchronous then $\tau_k = 0$ and the transmitted signal becomes:

$$S(t) = \sum_{k=1}^K s_k(t) = \sum_{k=1}^K \sqrt{\xi_k} \sum_{m=1}^M b_k(m) g_k(t - mT)$$

$$S(t) = \sum_{k=1}^K \sqrt{\xi_k} \sum_{m=1}^M b_k(m) \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} C_i e^{j2\pi f_i(t - (m + \frac{n}{L})T)} \quad (8)$$

We consider that the signal multiplexing OFDM is orthogonal. And if the space between the frequencies is $1/T_s$ then $f_i = f_0 + \frac{i}{T_s}$ and replacing C by its values, then:

$$S(t) = \sum_{k=1}^K \sqrt{\xi_k} \sum_{m=1}^M b_k(m) \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} (\alpha_i + j\beta_i) e^{j2\pi(f_0 + \frac{i}{T_s})(t - (m + \frac{n}{L})T)} \quad (9)$$

$$\text{And also } s_k(t) = \sqrt{\xi_k} \sum_{m=1}^M b_k(m) \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} (\alpha_i + j\beta_i) e^{j2\pi(f_0 + \frac{i}{T_s})(t - (m + \frac{n}{L})T)} \quad (10)$$

3- MULTIPLEXING OF SIGNALS WITH NOISE

Let a signal S(t) consisting of sequences S_k(t) and a noise B(t) be.

$$S(t) = \sum_{k=1}^K S_k(t) + B(t) \quad (11)$$

The signals S(t) form a discrete set of signals of finite energy E(S) of duration T_s.

$$E(S) = \int_0^{T_s} S^2(t) dt = \text{cte} \quad (12)$$

As any function or some random finite energy on (0, T_s) can be regarded as a vector of Hilbert, in case the noise introduced by the transmission; B_k projections are then random variables defined by equation (13):

$$B(t) = \sum_{k=1}^{\infty} B_k \cdot \varphi_k(t) \quad \text{avec } B_k = \langle \varphi_k, B \rangle \quad (13)$$

So we can rough estimate that : $S(t) = \sum_{k=1}^K S_k(t) + \sum_{k=1}^K B_k \varphi_k(t)$

$$S(t) = \sum_{k=1}^K (S_k(t) + B_k \varphi_k(t))$$

$$\text{With } s_k(t) = \sqrt{\xi_k} \sum_{m=1}^M b_k(m) \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} (\alpha_i + j\beta_i) e^{j2\pi(f_0 + \frac{i}{T_s})(t - (m + \frac{n}{L})T)} \quad (14)$$

Thus we have

$$S(t) = \sum_{k=1}^K \left(\sqrt{\xi_k} \sum_{m=1}^M b_k(m) \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} (\alpha_i + j\beta_i) e^{j2\pi(f_0 + \frac{i}{T_s})(t - (m + \frac{n}{L})T)} + B_k \varphi_k(t) \right)$$

$$S(t) = \sum_{k=1}^K \left(\sqrt{\xi_k} \sum_{m=1}^M b_k(m) \sum_{n=0}^{N-1} a_k(n) \sum_{i=0}^{L-1} (\alpha_i + j\beta_i) e^{j2\pi(f_0 + \frac{i}{T_s})(t - (m + \frac{n}{L})T)} + B_k \varphi_k(t) \right)$$

If we consider, that the noise introduced is Gaussian, then its spectral density is $\gamma(\nu) = \frac{N_0}{2}$ and the correlation function is thereby $C_B(\tau) = \frac{N_0}{2} \delta(\tau)$. Therefore, the noise $B(t)$ is represented by a random vector whose components are B_k . B is Gaussian random variables independent of the variance $\frac{N_0}{2}$.

4- OFDM SYSTEM

4.1. Principle

The principle of OFDM consists in dividing a stream of symbols at a rate $\frac{1}{T}$ symbol streams at the rate $\frac{1}{NT}$ each. And N symbols are transmitted in parallel over a period NT . The bandwidth is divided into N sub-bands below each to the coherence bandwidth of the channel (provided that N is sufficiently large), which explains the robustness of this modulation in the presence of frequency selective channels.

4.2. Advantages

OFDM has the following advantages:

- The main advantage of OFDM lies in the simplicity of the equalization of channel distortions. Contrary to single carrier systems in which attenuation correction of the channel requires a matrix inversion often complex to implement, OFDM has the ability to equalize this effect by simple multiplication by a coefficient of equalizer on each sub-carrier;
- In addition, in a single carrier system, when the sampling frequency increases, the number of coefficients to estimate the channel increases, and thus increases the complexity of the receiver itself, which is not the case for OFDM which requires just a single estimate whatever the sampling frequency may be;
- On the other hand, OFDM has an effective use of allocated frequency band using orthogonal carriers.

4.3. Disadvantages

OFDM has some disadvantages. We distinguish:

- OFDM has some weaknesses compared to single-carrier system. Indeed, a simple channel equalization in OFDM loses the diversity gain. In addition, a severe selective fading channel to a given carrier could lose the whole information posted on it [11] which explains the dramatic effect of performances of uncoded OFDM. Generally, methods based on coding (convolutional coding, diversity constellation, turbo code ...) are used with interleaving to combat such fading.
- So, OFDM is very sensitive to synchronization errors [12] [13]. They create interferences between subcarriers and destroy the orthogonality of subcarriers.
- Finally, OFDM is sensitive to nonlinear distortions introduced by the power amplifier of the transmitter, which destroys the orthogonality of subcarriers.

5- WB-CDMA TECHNOLOGY

WB-CDMA technology is the access code division multiple systems using direct sequence modulation (DS-WB-CDMA). This shows that the bits corresponding to user data are multiplied by a sequence of bits having particular characteristics over a wide bandwidth. Then,

there is a spread spectrum. This latter broadens the spectrum of a transmission to make it gain strength. It exists two families of codes:

- The channelization codes commonly called orthogonal codes to variable spreading factor (OVSF: Orthogonal Variable Spreading Factor) are characterized by their orthogonality, what is allowing the receiver to separate the signals transmitted on the same frequency band simultaneously;
- scrambling codes commonly called Scrambling codes are pseudo-random (PN: Pseudo Noise) characterized by a perfect autocorrelation property.

The functions of each type of code are summarized in Table 2.1.

Table 2.1. Features channelization codes and scrambling [2] and [14]

Functionalities	Code of channeling	Code of scrambling
Usage	<p>Uplink: Channel separation DPDCH and DPCCH from the same terminal.</p> <p>Downlink : Separation of connections of different users of the same cell</p>	<p>Uplink : Separation of the long terminal code sequence: $2^{24} - 1$</p> <p>Downlink : Cell separation code short sequence : $2^{18} - 1$</p>
Length	<p>Uplink : 4 à 252 chips (1 à 66,7µs)</p> <p>Downlink : 512 chips</p>	<p>Uplink : 10 ms =38 400 chips ou 66,7 µs=256 chips</p> <p>Downlink :10 ms =38 400 chips</p>
Number of codes	Number of codes equal to the spreading factor	<p>Uplink : several million</p> <p>Downlink : 512</p>
Family of codes	Orthogonal Variable Spreading Factor (OVSF)	<p>10 ms: Gold code</p> <p>66,7 µs: Extended S(2) code</p>
Spreading	<p>yes</p> <p>Increase the bandwidth</p>	<p>No</p> <p>No change in the bandwidth</p>

The term flow is $D = \frac{N.R}{T_s + \Delta} \log_2(M)$. (16)

In which N is the number of carrier, R is the efficiency of coding, Ts is the symbol duration, Δ is the guard interval and M is the number of states.

WB-CDMA technique which is reserved for transmission systems and digital signal processing must be able to support multimedia applications requiring broadband. For 64 QAM modulation in a yield of coding $R = 3/4$, $T_s=2.5\mu s$, $\Delta=0$, $N=1000$, the theoretical bandwidth available can reach up to 22.5 Mbit/s.

This system is possible through the use of OFDM (Orthogonal Frequency Division Multiplexing).

We have studied the evolution of the flow depending on the number of carriers and taking into account the bit error rate (BER) (17):

$$TEB = 4 \left(1 - \frac{1}{\sqrt{M}} \right) \cdot \frac{1}{2} \operatorname{erfc}(\sqrt{\gamma}) \text{ with } \gamma = \frac{E_b}{N_0} \gamma \text{ is the signal to noise ratio.}$$

From equation (17), we derive the number of states M (18)

$$M = \left(\frac{1}{1 - \frac{TEB}{2 \operatorname{erfc}(\sqrt{\gamma})}} \right)^2 \quad (18)$$

By replacing M by its expression in the relationship (16) giving flow, we have finally the relationship between flow rate and the number of carriers set by the bit error rate BER (19).

$$D = \frac{2.N.R}{T_s + \Delta} \log_2 \left(\frac{1}{1 - \frac{TEB}{2 \operatorname{erfc}(\sqrt{\gamma})}} \right) \quad (19)$$

Figure 1 shows the evolution of the flow depending on the number of carriers for values of bit error rate fixed.

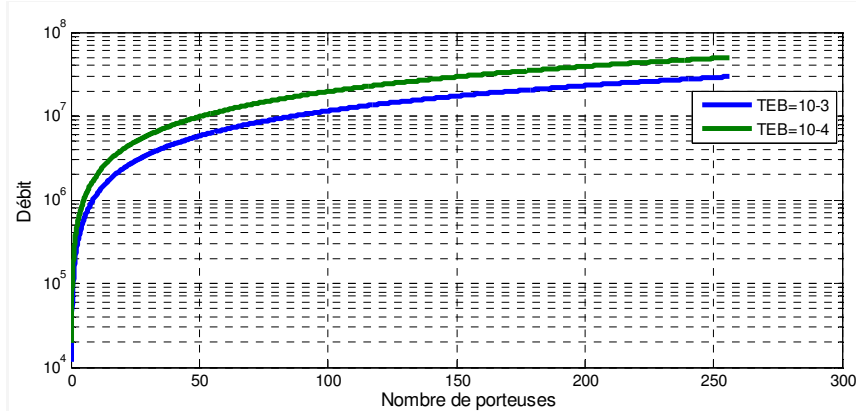


Figure 1: the flow depending on the number of carriers set by the BER.

We note that reducing the bit error rate increases the rate which is based on the number of carriers. UTRAN-FDD mode is based on the multiple access technique WB-CDMA technology which corresponds to the DS-SS (Direct Sequence Spread Spectrum) with a spread over a 5 MHz bandwidth [2]. The frequency range of UMTS is [1920 - 1980 MHz] for the uplink bandwidth and [2110 - 2170 MHz] for the downlink bandwidth [2][3].

6- RESULTS OF THE USE OF MULTIPLEXING OFDM SIGNALS IN A UMTS NETWORK

As the Fourier transform of a real function is the power spectrum is an even and symmetrical function. But it also includes negative frequencies.

The simulation results of the power spectrum are presented in two (02) categories: first, the power (dBm) is positive. So an "amplification" is in question. Figures 2, 3 and 4 respectively illustrate the frequency spectrum of a carrier and different carriers, the frequency spectrum of a function and the signal for 10 carriers OFDM and OFDM signal spectrum for 15 and 20 carriers.

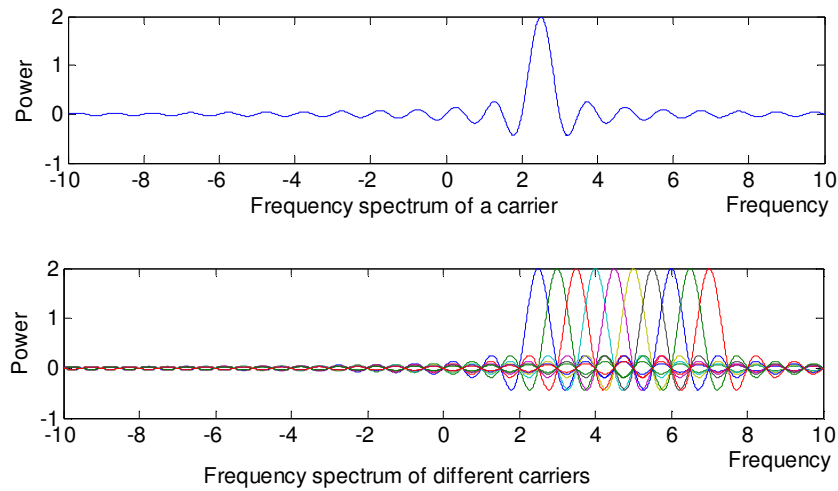


Figure 2: Spectrum of a carrier frequency and different carriers

The overlay spectra $S_k(f)$ ($k = 1$ to 10) shows that one of these spectra is at maximum while others are stabilized at zero (0) and also at this level that there is a partial recovery of the next spectrum. As the frequencies are orthogonal, it is assumed that the B band signal is constant while increasing the number of carriers does not increase the flow because $B = 1/T_s$ $B=1/T_s$ $=\Delta f$, but the spacing between carriers (Δf) decreases. And if (Δf) is constant, then increase the number of carriers increased throughput but also the signal band.

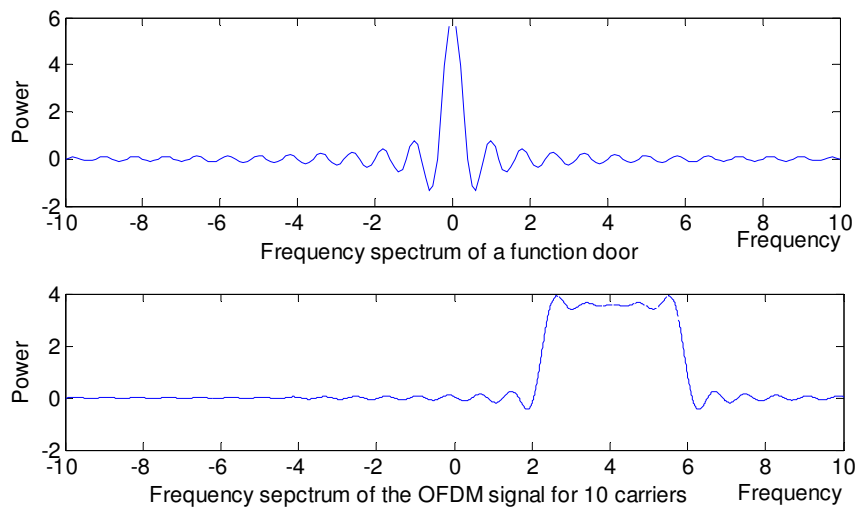


Figure 3: Frequency Spectrum of a function of the OFDM signal door and for 10 carriers

We see that, the spectrum $S(f)$ of the 10 carrier OFDM signal has a bandwidth (between 2.05 and 6.11) much higher than spectrum function is (between -0.5 and 0.5).

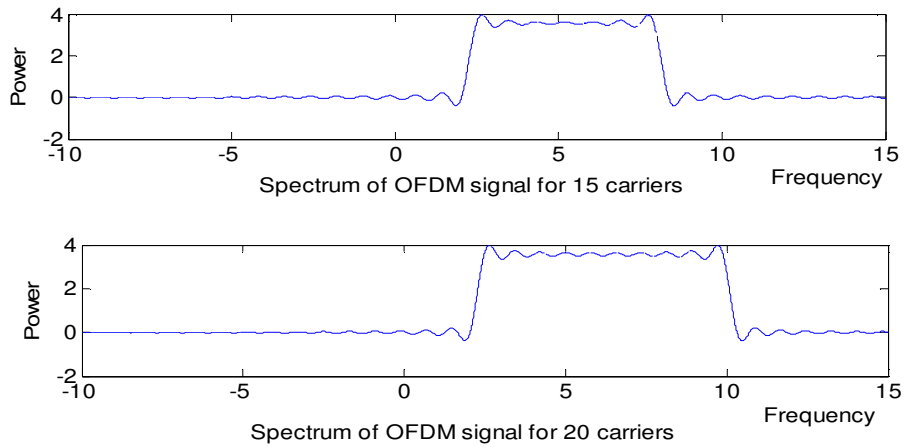


Figure 4: Spectrum of OFDM signal for 15 and 20 carriers.

We note that the bandwidth of 20 carriers (between 2.05 and 10.31) is greater than 15 carriers (between 2.05 and 8.35). Therefore, the greater the number of carriers is, the greater is the size of the spectrum.

And secondly, the power (dBm) is negative, then one speaks of a "mitigation". Figure 5 and Figure 6 show respectively the attenuation spectrum of a carrier and the various carriers and the attenuation of a spectrum is a function of the OFDM signal and for 10 carriers.

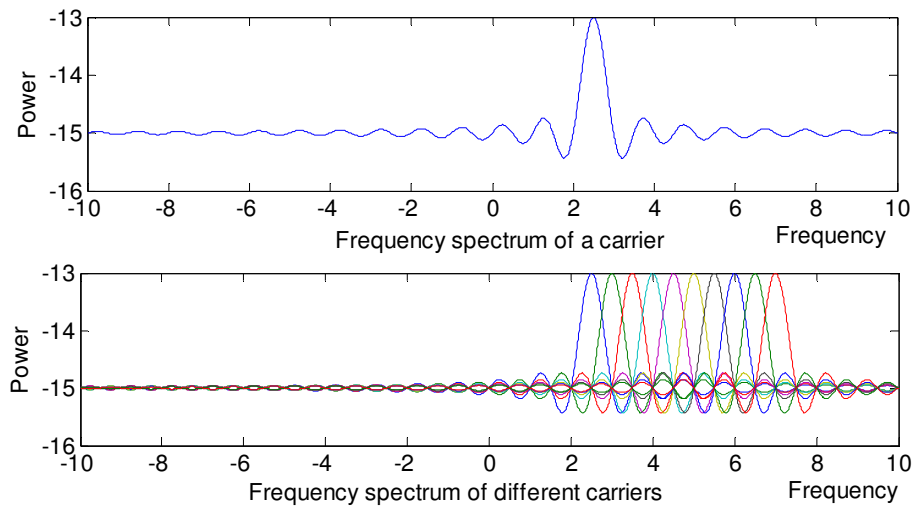


Figure 5: The attenuation spectrum of a carrier and different carriers

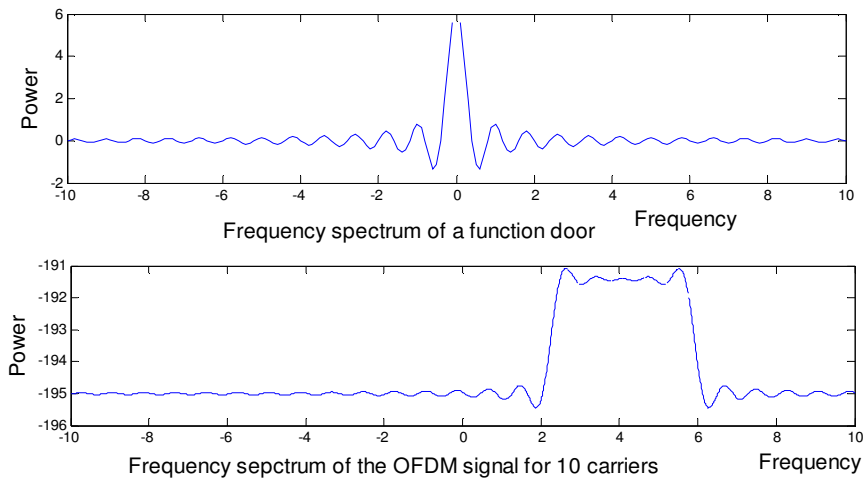


Figure 6: Attenuation of a spectrum of a function of the door and for 10 carrier OFDM signal

We note that, on the last two figures, the power had some negative values whatever the value of the frequency spectrum but the shape remains almost the same as Figure 2, Figure 3 and Figure 4.

We point out to your attention that the multiplication of the power spectrum by an equal number of +1 or -1 does not change its power.

7- CONCLUSION

In this paper, we made a study of multiplexing signals on the downlink OFDM in UTRAN-FDD simulation. The results show that the power spectrum of an OFDM signal is centered around its fundamental frequency. But also the sum of power spectra of OFDM signals has a bandwidth greater than that of a power spectrum function which was used in the past. So the use of OFDM signals by the simulation allowed us to improve the flow, which was estimated at 2 Mbit/s to 22.5 Mbit/s.

Finally, the more the number of carriers increase, the more the band of spectrum is important and the more status and more QAM increases the data rate.

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