# Different node deployments in a square area grid of wireless sensor network and optimal number of relays 

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#### Abstract

Wireless sensor networks deployment is an important issue to be considered when trying to cover an area with sensors, our work focuses on the deployment of a grid network for larger number of sensor nodes from 36 nodes up to 100 nodes. We study different cases of distances between source an destination, the result showed the diagonal path is the best path where least energy consumption are consumed. The diagonal path use number of intermediate nodes (relays) along it. Our result show the best number of relay nodes and different distances between source node and destination node according to some threshold distances.


## Keywords

Node deployment, relay nodes, power consumption.

## 1. Introduction

A wireless sensor network is a collection of sensor nodes which are consist of sensing unit, processing unit, transceiver unit, and power unit [1]. The sensor nodes collect the data from its environment and send the collected data to the single hop neighboring nodes which in turn send this data to the sink node [2]. Sensor nodes deployment is an important issue in terms of coverage, connectivity, cost and lifetime [3]. In [4-7] the deployment issue with ensuring network connectivity and system lifetime maximization where very well investigated. In [8] the authors discussed the optimal power consumption in cooperative WSNs where nodes are deployed in grid manner for $2 \times 2$ network ( 4 nodes) up to $5 \times 5$ grid network ( 25 node). Power consumption is a very important issue that should be taken into account when deploying nodes in a field. In this paper we discuss the power consumption with different cases of node deployment in grid of network of $6 \times 6$ up to $10 \times 10$ network. The rest of this paper is organized as follows: In section 2, energy analysis of wireless transmission and network model are presented, in the next section, the experimental results are analyzed, and discussion and conclusion are given in section 4 .

## 2. Energy analysis of wireless transmission and network model

To transmit a data from the source node to the destination node, number of relay nodes can be used to reduce the power consumption required for the transmission. These relay nodes will act as a router which receive the data, amplify the data signal and forward it to next neighbor. Receiving, amplifying, and forwarding data can be expressed by the following models [9, 11]:

$$
\begin{align*}
& E T x  \tag{1}\\
&(k, d)= E T x_{-} \text {elec } \times K+\varepsilon a m p \times K \times d^{2}  \tag{2}\\
& E R x(K)=E R x_{-} \text {elec }
\end{align*}
$$

Where:
ETx $(k, d)$ : Power consumption in transmission of $K$ bits for distance $d$
$E R x(K)$ : Power consumption in reception of $K$ bits
ERx_elec : Power consumption in the sensor node receiver circuit to process 1 bit
ETx_elec : Power consumption in the sensor node transmitter circuit to process 1 bit
$\varepsilon$ amp: Power consumption by amplifier
$K$ : Data size in bits
d: Distance between the two nodes
We use static nodes that are equally spaced from each other in 2-d grid network [10]. The following parameters are used:
N : The total number of nodes in the network ( $36,49,64,81$ and 100) node.
d row: The distance from the first node to the last node in the same row/column (in meters).
K: 1-bit.

## 3. Experimental results

For all cases ( $6 \mathrm{x} 6,7 \mathrm{x} 7,8 \mathrm{x} 8,9 \mathrm{x} 9$ and 10x10), we use $a m p=100 \mathrm{pJ} / \mathrm{bit} / \mathrm{m} 2$, ERX_elec $=50$ $\mathrm{nJ} / \mathrm{bit}$, ETX_elec $=50 \mathrm{~nJ} / \mathrm{bit}$ as in $[8,12]$ for calculating the power consumption represented by (1) and (2). Also we assume the source node and the destination node are the two farthest nodes in the grid that sends and receives data along the diagonal path.

### 3.1 Analysis and experimental result of 6x6 network:

We assume source node 1 sends data to destination node 36 as in figure 1 .
Case 1: direct path from node 1 to node 36 without any relay, noting that the distance from node 1 to node 36 is $\sqrt{2}$ drow:

$$
\begin{equation*}
\text { E6x6 }- \text { direct }=2 \times 0.1 \text { drow }^{2}+100 \tag{3}
\end{equation*}
$$

Case2: By using relay nodes:

## For one relay case:

- Node 8 = node 29 because each of them has one short transmission and four long transmission blocks. So the total power consumption after applying (1) and (2) is:

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$$
\begin{equation*}
\mathrm{E} 6 \times 6=\frac{3.4}{25} \text { drow }^{2}+200 \tag{4}
\end{equation*}
$$

- Node $15=$ node 22 :

$$
\begin{equation*}
\mathrm{E} 6 \mathrm{x} 6=\frac{2.6}{25} \mathrm{drow}^{2}+200 \tag{5}
\end{equation*}
$$

| 31 | 32 | 33 | 34 | 35 | 36 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 25 | 26 | 27 | 28 | 29 | 30 |
| 19 | 20 | 21 | 22 | 23 | 24 |
| 13 | 14 | 15 | 16 | 17 | 18 |
| 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 2 | 3 | 4 | 5 | 6 | drow

Figure1: wireless sensor nodes in $6 \times 6$ deployment

## For two relays case:

$-\operatorname{Nodes}(8,15)=(8,29)=(22,29)$ :

$$
\begin{equation*}
\mathrm{E} 6 \mathrm{x} 6=\frac{2.2}{25} \mathrm{drow}^{2}+300 \tag{6}
\end{equation*}
$$

- Nodes $(8,22)=(15,22)=(15,29)$ :

$$
\begin{equation*}
\mathrm{E} 6 \mathrm{x} 6=\frac{1.8}{25} \mathrm{drow}^{2}+300 \tag{7}
\end{equation*}
$$

## For three relays case:

$-\operatorname{Nodes}(8,15,22)=(8,15,29)=(8,22,29)=(15,22,29)$ :

$$
\begin{equation*}
\mathrm{E} 6 \mathrm{x} 6=\frac{1.4}{25} \text { drow }^{2}+400 \tag{8}
\end{equation*}
$$

## For four relays case:

- Nodes $(8,15,22,29)$ :

$$
\begin{equation*}
\mathrm{E} 6 \times 6=\frac{1}{25} \mathrm{drow}^{2}+500 \tag{9}
\end{equation*}
$$

For the case of $6 \times 6$ we will have the following four lemmas:

## Lemma 1:

Threshold distance between the optimal power consumption using direct path and using one relay (in the middle either node 15 or 22) in $6 \times 6$ grid is 32.27 m .

## Proof:

Set (3) and (5) together to get:
2 X 0.1 drow $^{2}+100=\frac{2.6}{25} \mathrm{drow}^{2}+200$
Implies: drow $=32.27 \mathrm{~m}$.

## Lemma 2:

Threshold distance between the optimal power consumption using one relay path (middle) and using two relays (node 15 and 22) in $6 \times 6$ grid is 56 m .

## Proof:

Set (5) and (7) together to get:
$\frac{2.6}{25}$ drow $^{2}+200=\frac{1.8}{25}$ drow $^{2}+300$
Implies: drow $\cong 56 \mathrm{~m}$

## Lemma 3:

Threshold distance between the optimal power consumption using two and three relays in $6 \times 6$ grid is 79 m .

## Proof:

Set (7) and (8) together to get:

$$
\frac{1.8}{25} \mathrm{drow}^{2}+300=\frac{1.4}{25} \mathrm{drow}^{2}+400
$$

Implies: drow $\cong 79 \mathrm{~m}$

## Lemma 4:

Threshold distance between the optimal power consumption using three and four relays in $6 \times 6$ grid is 79 m .

## Proof:

Set (8) and (9) together to get:
$\frac{1.4}{25}$ drow $^{2}+400=\frac{1}{25}$ drow $^{2}+500$
Implies: drow $\cong 79 \mathrm{~m}$.
In $6 \times 6$ grid network, we notice that direct path is best up to 32.27 m , then using one relay would give better power consumption for up to distance 56 m , and then four relays would be the choice for distance longer than 79 m .

### 1.2 Analysis and experimental results of 7x7 deployment:

We assume source node 1 sends data to destination node 49 as in figure2:
Case 1: direct path from node 1 to node 49 without any relay:

$$
\begin{equation*}
\mathrm{E} 7 \times 7-\text { direct }=2 \mathrm{X} 0.1 \text { drow }^{2}+100 \tag{10}
\end{equation*}
$$

Case2: As in $6 \times 6$ deployment, number of relay nodes exist, but the most optimal relay nodes that consume less transmission blocks are:

## For one relay case:

- Node 25:

$$
\begin{equation*}
\mathrm{E} 7 \mathrm{x} 7=\frac{3.6}{36} \mathrm{drow}^{2}+200 \tag{11}
\end{equation*}
$$

| 43 | 44 | 45 | 46 | 47 | 48 | 49 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | drow

Figure2: wireless sensor nodes in 7 x 7 deployment

## For two relays case:

- Nodes $(17,33)$ :

$$
\begin{equation*}
\mathrm{E} 7 \mathrm{x} 7=\frac{2.4}{36} \mathrm{drow}^{2}+300 \tag{12}
\end{equation*}
$$

## For three relays case:

$-\operatorname{Nodes}(9,17,33)=(9,25,33)=(9,25,41)=(17,25,33)=(17,25,41)=(17,33,41)$ :

$$
\begin{equation*}
\mathrm{E} 7 \mathrm{x} 7=\frac{2}{36} \text { drow }^{2}+400 \tag{13}
\end{equation*}
$$

## For four relays case:

- Nodes $(9,17,25,33)=(9,17,25,41)=(9,17,33,41)=(9,25,33,41)=(17,25,33,41)$ :

$$
\begin{equation*}
\mathrm{E} 7 \mathrm{x} 7=\frac{1.6}{36} \mathrm{drow}^{2}+500 \tag{14}
\end{equation*}
$$

## For five relays case:

- Nodes $(9,17,25,33,41)$ :

$$
\begin{equation*}
\mathrm{E} 7 \times 7=\frac{1.2}{36} \text { drow }^{2}+600 \tag{15}
\end{equation*}
$$

For the case of 7 x 7 we will have the following five lemmas:

## Lemma 5:

Threshold distance between the optimal power consumption using direct path and using one relay in 7 x 7 grid is 31.62 m .

Proof:
Set (10) and (11) together to get:
2 X 0.1 drow $^{2}+100=\frac{3.6}{36}$ drow $^{2}+200$
Implies: drow $=31.62 \mathrm{~m}$.

## Lemma 6:

Threshold distance between the optimal power consumption using one and two relays in 7 x 7 grid is 54.77 m .

## Proof:

Set (11) and (12) together to get:
$\frac{3.6}{36}$ drow $^{2}+200=\frac{2.4}{36}$ drow $^{2}+400$
Implies: drow $=54.77 \mathrm{~m}$.

## Lemma 7:

Threshold distance between the optimal power consumption using two relays and three relays in 7 x 7 grid is 94.86 m .

## Proof:

Set (12) and (13) together to get:
$\frac{2.4}{36} \mathrm{drow}^{2}+300=\frac{2}{36}$ drow $^{2}+400$
Implies: drow $=94.86 \mathrm{~m}$.

## Lemma 8:

Threshold distance between the optimal power consumption using three relays and using four relays in 7 x 7 grid is 94.86 m .

## Proof:

Set (13) and (14) together to get:
$\frac{2}{36}$ drow $^{2}+400=\frac{1.6}{36}$ drow $^{2}+500$
Implies: drow $=94.86 \mathrm{~m}$.

## Lemma 9:

Threshold distance between the optimal power consumption using four and five relays in 7 x 7 grid is 94.86 m .

## Proof:

Set (14) and (15) together to get:
$\frac{1.6}{36}$ drow $^{2}+500=\frac{1.2}{36}$ drow $^{2}+600$
Implies: drow $=94.86 \mathrm{~m}$.
In $7 \times 7$ grid network, we notice that direct transmission is best up to 31.62 m , after that one relay would give better power consumption up to distance 54.77 m , and then five relays would be the choice for distances longer than 94.86 m .

### 3.2 Analysis and experimental results of $8 \times 8$ deployment:

We assume source node 1 sends data to destination node 64 as in figure3:

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| 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 |
| 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 |
| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | drow

Figure 3: wireless sensor nodes in 8 x 8 deployment
Case 1: direct path from node 1 to node 64 without any relay:

$$
\begin{equation*}
\mathrm{E} 8 \times 8-\text { direct }=2 \times 0.1 \text { drow }^{2}+100 \tag{16}
\end{equation*}
$$

Case2: By using relay nodes:

## For one relay:

- Node $28=$ node 37 :

$$
\begin{equation*}
\mathrm{E} 8 \mathrm{x} 8=\frac{5}{49} \mathrm{drow}^{2}+200 \tag{17}
\end{equation*}
$$

## For two relays case:

- Nodes $(19,37)=(19,46)=(28,46)$ :

$$
\begin{equation*}
\mathrm{E} 8 \mathrm{x} 8=\frac{3.4}{49} \mathrm{drow}^{2}+300 \tag{18}
\end{equation*}
$$

## For three relays case:

$-\operatorname{Nodes}(10,28,46)=(19,28,46)=(19,37,46)=(19,37,55):$

$$
\begin{equation*}
\mathrm{E} 8 \mathrm{x} 8=\frac{2.6}{49} \mathrm{drow}^{2}+400 \tag{19}
\end{equation*}
$$

## For four relays case:

- $\quad$ Node $(10,19,28,46)=(10,19,37,55)=(10,28,37,46)=(10,28,46,55)=(10,28,37,55)=$ $(19,28,37,46)=(19,28,37,55)=(19,37,46,55)=(19,28,46,55):$

$$
\begin{equation*}
\mathrm{E} 8 \mathrm{x} 8=\frac{2.2}{49} \mathrm{drow}^{2}+500 \tag{20}
\end{equation*}
$$

## For five relays case:

- Nodes $(10,19,28,37,46)=(10,19,28,37,55)=(10,19,28,46,55)=(10,19,37,46,55)=$ $(10,28,37,46,55)=(19,28,37,46,55):$

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$$
\begin{equation*}
\mathrm{E} 8 \mathrm{x} 8=\frac{1.8}{49} \mathrm{drow}^{2}+600 \tag{21}
\end{equation*}
$$

## For six relays case:

- Nodes (10,19,28,37,46,55):

$$
\begin{equation*}
\mathrm{E} 8 \mathrm{x} 8=\frac{1.4}{49} \text { drow }^{2}+700 \tag{22}
\end{equation*}
$$

For the case of $8 x 8$ we will have the following six lemmas:

## Lemma 10:

Threshold distance between the optimal power consumption using direct path and using one relay in 8 x 8 grid is 33.33 m .

## Proof:

Set (16) and (17) together to get:
2 X 0.1 drow $^{2}+100=\frac{5}{49}$ drow $^{2}+200$
Implies: drow $=33.33 \mathrm{~m}$.

## Lemma 11:

Threshold distance between the optimal power consumption using one and relays in $8 \times 8$ grid is 55.33 m .
Proof:
Set (17) and (18) together to get:
$\frac{5}{49} \mathrm{drow}^{2}+200=\frac{3.4}{49} \mathrm{drow}^{2}+300$
Implies: drow $=55.33 \mathrm{~m}$.

## Lemma 12:

Threshold distance between the optimal power consumption using two and three relays in $8 \times 8$ grid is 78.26 m .

## Proof:

Set (18) and (19) together to get:
$\frac{3.4}{49}$ drow $^{2}+300=\frac{2.6}{49}$ drow $^{2}+400$
Implies: drow $=78.26 \mathrm{~m}$.

## Lemma 13:

Threshold distance between the optimal power consumption using three and four relays in 8 x 8 grid is 110.67 m .

## Proof:

Set (19) and (20) together to get:
$\frac{2.6}{49}$ drow $^{2}+400=\frac{2.2}{49}$ drow $^{2}+500$
Implies: drow= 110.67 m .

## Lemma 14:

Threshold distance between the optimal power consumption using four and five relays in $8 \times 8$ grid is 110.67 m .

## Proof:

Set (20) and (21) together to get:
$\frac{2.2}{49}$ drow $^{2}+500=\frac{1.8}{49}$ drow $^{2}+600$
Implies: drow= 110.67 m .

## Lemma 15:

Threshold distance between the optimal power consumption using five and six relays in $8 \times 8$ grid is 110.67 m .

## Proof:

Set (21) and (22) together to get:
$\frac{1.8}{49}$ drow $^{2}+600=\frac{1.4}{49}$ drow $^{2}+700$
Implies: drow= 110.67 m .
In $8 \times 8$ grid network, we notice that direct transmission is good up to 33.33 m , then one relay is better for distances up to 55.33 , two relays would be the choice for distance up to 78.26 m , and then six relays would give best power consumption for distances longer than 110.67 m .

### 3.3 Analysis and experimental results of $\mathbf{9 x} \mathbf{9}$ deployment:

We assume source node 1 sends data to destination node 81 as in figure4:
Case 1: direct path from node 1 to node 81 without any relay:

$$
\begin{equation*}
\text { E9x9 - direct }=2 \times 0.1 \text { drow }^{2}+100 \tag{23}
\end{equation*}
$$

Case2: By using relay nodes:

## For one relay case:

- Node 41

$$
\begin{equation*}
E 9 x 9=\frac{6.4}{64} \text { drow }^{2}+200 \tag{24}
\end{equation*}
$$

## For two relays case:

- $\operatorname{Nodes}(11,41)=(31,41)=(31,71)=(41,51)=(41,71)=(11,51)$ :

$$
\begin{equation*}
\mathrm{E} 9 \mathrm{x} 9=\frac{5.2}{64} \mathrm{drow}^{2}+300 \tag{25}
\end{equation*}
$$

## For three relays case: 8

$-\operatorname{Nodes}(11,21,51)=(11,41,51)=(11,41,71)=(31,41,51)=(31,41,71)=(31,61,71)$ :

$$
\begin{equation*}
\mathrm{E} 9 \mathrm{x} 9=\frac{4}{64} \mathrm{drow}^{2}+400 \tag{26}
\end{equation*}
$$

| 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 |
| 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 |
| 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 |
| 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 |
| 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 |
| 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | drow

Figure4: wireless sensor nodes in 9x9 deployment

## For four relays case:

- Nodes $(11,21,31,51)=(11,21,31,61)=(11,21,41,51)=(11,21,41,71)=(11,21,51,61)=$ $(11,21,51,71)=(11,31,41,51)=(11,31,41,71)=(11,41,51,61)=(11,4151,71)=(11,41,61,71)$ $=(21,31,41,51)=(21,31,41,71)=(21,51,61,71)=(31,41,51,61)=(31,41,51,71)=$ $(31,41,61,71)=(31,51,61,71)=(11,31,61,71)$ :

$$
\begin{equation*}
\mathrm{E} 9 \mathrm{x} 9=\frac{3.2}{64} \mathrm{drow}^{2}+500 \tag{27}
\end{equation*}
$$

## For five relays case:

- $\operatorname{Nodes}(11,21,31,41,61)=(11,21,31,51,61)=(11,21,3151,71)=(11,21,41,51,61)=$ $(11,21,41,51,71)=(11,21,41,61,71)=(11,31,41,51,61)=(11,31,41,51,71)=(11,31,51,61,71)$ $=(21,31,41,51,61)=(21,31,41,51,71)=(21,31,41,61,71)=(21,31,51,61,71)=$ (21,41,51,61,71):

$$
\begin{equation*}
\mathrm{E} 9 \mathrm{x} 9=\frac{2.4}{64} \mathrm{drow}^{2}+600 \tag{28}
\end{equation*}
$$

## For six relay nodes case:

- Nodes $(11,21,31,41,51,61)=(11,21,31,41,51,71)=(11,21,31,51,61,71)=$ $(11,21,41,51,61,71)=(11,31,41,51,61,71)=(21,31,41,51,61,71)$ :

$$
\begin{equation*}
\mathrm{E} 9 \mathrm{x} 9=\frac{2}{64} \mathrm{drow}^{2}+700 \tag{29}
\end{equation*}
$$

For seven relay nodes: $(11,21,31,41,51,61,71)$ :

$$
\begin{equation*}
\mathrm{E} 9 \mathrm{x} 9=\frac{1.6}{64} \mathrm{drow}^{2}+800 \tag{30}
\end{equation*}
$$

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For the case of $9 \times 9$ we will have the following seven lemmas:

## Lemma 16:

Threshold distance between the optimal power consumption using direct transmission and one relay in 9 x 9 grid is 31.62 m .

Proof:
Set (23) and (24) together to get:
2 X 0.1 drow $^{2}+100=\frac{6.4}{64}$ drow $^{2}+200$
Implies: drow=31.62 m.

## Lemma 17:

Threshold distance between the optimal power consumption using one and two relays in 9 x 9 grid is 73 m .

## Proof:

Set (24) and (25) together to get:
$\frac{6.4}{64}$ drow $^{2}+200=\frac{5.2}{64}$ drow $^{2}+300$
Implies: drow= 73 m .

## Lemma 18:

Threshold distance between the optimal power consumption using two and three relays in 9 x 9 grid is 73 m .
Proof:
Set (25) and (26) together to get:
$\frac{5.2}{64}$ drow $^{2}+300=\frac{4}{64}$ drow $^{2}+400$
Implies: drow=73m.

## Lemma 19:

Threshold distance between the optimal power consumption using three and four relays in 9 x 9 grid is 89.44 m .
Proof:
Set (26) and (27) together to get:
$\frac{4}{64} \mathrm{drow}^{2}+400=\frac{3.2}{64} \mathrm{drow}^{2}+500$
Implies: drow $=89.44 \mathrm{~m}$

## Lemma 20:

Threshold distance between the optimal power consumption using four and five relays in 9 x 9 grid is 89.44 m .

## Proof:

Set (27) and (28) together to get:
$\frac{3.2}{64}$ drow $^{2}+500=\frac{2.4}{64}$ drow $^{2}+600$
Implies: drow $=89.44 \mathrm{~m}$.
Lemma 21:
Threshold distance between the optimal power consumption using five and six relays in 9 x 9 grid is 126.5 m .

## Proof:

Set (28) and (29) together to get:
$\frac{2.4}{64}$ drow $^{2}+600=\frac{2}{64}$ drow $^{2}+700$
Implies:
drow $=126.5 \mathrm{~m}$.

## Lemma 22:

Threshold distance between the optimal power consumption using six and seven relays in $9 \times 9$ grid is 126.5 m .

## Proof:

Set (29) and (30) together to get:
$\frac{2}{64}$ drow $^{2}+700=\frac{1.6}{64}$ drow $^{2}+800$
Implies: drow $=126.5 \mathrm{~m}$.
In 9x9 grid network, we notice that direct transmission is best up to 31.62 m , then three relays is better for distance up to 73 m , five relays would be the choice for up to distance 89.44 m . seven relays would give the optimal power consumption for distances longer than 126.5 m .

### 3.4 Analysis and experimental results of $10 \times 10$ deployment:

We assume source node 1 sends data to destination node 100 as in figure 5:
Case 1: direct path from node 1 to node 100 without any relay:

$$
\begin{equation*}
\mathrm{E} 10 \times 10-\text { direct }=2 \times 0.1 \text { drow }^{2}+100 \tag{31}
\end{equation*}
$$

Case2: By using relay nodes:

## For one relay case:

- Node 45=56:

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{8.2}{81} \mathrm{drow}^{2}+200 \tag{32}
\end{equation*}
$$

## For two relays case:

- Nodes $(34,67)$ :

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{5.4}{81} \text { drow }^{2}+300 \tag{33}
\end{equation*}
$$

| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 61 | 62 | 63 | 64 | 65 | 67 | 67 | 68 | 69 | 70 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | drow

Figure5: wireless sensor nodes in $10 \times 10$ deployment

## For three relays case:

$-\operatorname{Nodes}(34,56,78)=(23,56,78)=(23,45,78)=(23,45,67)$ :

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{4.2}{81} \mathrm{drow}^{2}+400 \tag{34}
\end{equation*}
$$

## For four relays case:

- Nodes (
$12,34,56,78)=(23,34,56,78)=(23,45,56,78)=(23,45,67,78)=(23,45,67,89)=(23,56,67,78)$ $=(23,56,67,89)$ :

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{3.4}{81} \mathrm{drow}^{2}+500 \tag{35}
\end{equation*}
$$

## For five relays case:

- Nodes $(12,23,34,56,78)=(12,23,45,56,89)=(12,23,45,67,78)=(12,23,45,67,89)=$ $(12,34,45,67,78)=(12,34,45,67,89)=(12,34,56,67,78)=(12,34,56,67,89)=$ $(12,34,56,78,89)=(23,34,45,56,78)=(23,34,45,67,78)=(23,34,56,67,78)=$ $(23,34,56,67,89)=(23,34,56,78,89)=(23,45,56,67,78)=(23,45,56,67,89)=$ $(23,45,67,78,89)$ :

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{3}{81} \mathrm{drow}^{2}+600 \tag{36}
\end{equation*}
$$

## For six relay nodes case:

- Nodes $(12,23,34,45,56,78)=(12,23,34,45,56,78)=(12,23,34,45,67,89)=$ $(12,23,34,56,67,78)=(12,23,34,56,67,89)=(12,23,34,56,78,89=(12,23,34,67,78,89)=$

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$$
\begin{aligned}
& (12,23,45,56,67,78)=(12,23,45,56,67,89)=(12,23,45,56,78,89)=(12,23,45,67,78,89)= \\
& (23,34,45,56,67,78)=(23,34,45,56,67,89)=(23,34,45,56,78,89)=(23,34,45,67,78,89)= \\
& (23,34,56,67,78,89)=(23,45,56,67,78,89):
\end{aligned}
$$

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{2.6}{81} \text { drow }^{2}+700 \tag{37}
\end{equation*}
$$

## for seven relay nodes case:

- $\operatorname{Nodes}(12,23,34,45,56,67,78)=(12,23,34,45,56,67,89)=(12,23,34,45,56,78,89)=$
$(12,23,34,45,67,78,89)=(12,23,34,56,67,78,89)=(12,23,45,56,67,78,89)=$
$(12,34,45,56,67,78,89)=(23,34,45,56,67,78,89):$

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{2.2}{81} \mathrm{drow}^{2}+800 \tag{38}
\end{equation*}
$$

## For eight relay nodes:

- Nodes (12,23,34,45,56,67,78,89):

$$
\begin{equation*}
\mathrm{E} 10 \times 10=\frac{1.8}{81} \text { drow }^{2}+900 \tag{39}
\end{equation*}
$$

For $10 \times 10$ grid deployment we will have the following eight lemmas:

## Lemma 23:

Threshold distance between the optimal power consumption using direct transmission and one relay in $10 \times 10$ grid is 33.33 m .

## Proof:

Set (31) and (32) together to get:
2 X 0.1 drow $^{2}+100=\frac{8.2}{81}$ drow $^{2}+200$
Implies: drow $=33.33 \mathrm{~m}$.

## Lemma 24:

Threshold distance between the optimal power consumption using one and two relays in $10 \times 10$ grid is 53.78 m .

## Proof:

Set (32) and (33) together to get:
$\frac{8.2}{81}$ drow $^{2}+200=\frac{5.4}{81}$ drow $^{2}+300$
Implies: drow $=53.78 \mathrm{~m}$.

## Lemma 25:

Threshold distance between the optimal power consumption using two and three relays in $10 \times 10$ grid is 82.15 m .

## Proof:

Set (33) and (34) together to get:

$$
\frac{5.4}{81} \text { drow }^{2}+300=\frac{4.2}{81} \text { drow }^{2}+400
$$

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Implies: drow $=82.15 \mathrm{~m}$.

## Lemma 26:

Threshold distance between the optimal power consumption using three and four relays in10x 10 grid is 100.62 m .

## Proof:

Set (34) and (35) together to get:
$\frac{4.2}{81}$ drow $^{2}+400=\frac{3.4}{81}$ drow $^{2}+500$
Implies: drow $=100.62 \mathrm{~m}$.

## Lemma 27:

Threshold distance between the optimal power consumption using four and five relays in $10 \times 10$ grid is 142 m .

## Proof:

Set (35) and (36) together to get:
$\frac{3.4}{81}$ drow $^{2}+500=\frac{3}{81}$ drow $^{2}+600$
Implies: drow $=142 \mathrm{~m}$.

## Lemma 28:

Threshold distance between the optimal power consumption using five and six relays in $10 \times 10$ grid is 142 m .

## Proof:

Set (36) and (37) together to get:
$\frac{3}{81}$ drow $^{2}+600=\frac{2.6}{81}$ drow $^{2}+700$
Implies: drow $=142 \mathrm{~m}$.

## Lemma 29:

Threshold distance between the optimal power consumption using six and seven relays in $10 \times 10$ grid is 142 m .

## Proof:

Set (37) and (38) together to get:
$\frac{2.6}{81}$ drow $^{2}+700=\frac{2.2}{81}$ drow $^{2}+800$
Implies: drow $=142 \mathrm{~m}$.

## Lemma 30:

Threshold distance between the optimal power consumption using seven relays and eight relays in $10 \times 10$ grid is 142 m .
Proof:

Set (38) and (39) together to get:
$\frac{2.2}{81}$ drow $^{2}+800=\frac{1.8}{81}$ drow $^{2}+900$
Implies: drow $=142 \mathrm{~m}$.
In $10 \times 10$ grid network, we notice that direct transmission is best up to distance 33.33 m , then one relay node can be used up to distance 53.78 m , then two relays is better for distance 82.15 m , for up to 100.62 m three relays would be the choice, and finally for distance longer than 142 m , seven relays is the best.

## 4. Discussion and conclusion :

The direct transmission consumes much energy than using relays [8], so it is preferable to use efficient number of relays when transmitting from source to destination in order to reduce energy consumption to minimum. We studied the different cases of node deployment form $6 \times 6$ to $10 \times 10$ grid networks. The result shows that there are number of paths that the data can follow to be received by the destination, each of our selected paths to be as an optimal path consumes less energy than other paths.We explained what these paths are and which one is the best depending on the shortest transmission block.

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